



Large Mode Area Photonic Crystal Fiber with Low Dispersion and Confinement Loss for Terahertz Wave Guiding

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Abstract: A photonic crystal fiber (PCF) made of the cyclic-olefin copolymer (COC) with low dispersion and confinement loss, large-mode-area, and single-mode transmission for terahertz wave guiding is described. The characteristics of the PCF in the terahertz range are simulated and analyzed by the full-vector finite element method (FEM). The effects of the structural parameters on the performance of the terahertz PCF are also investigated. The effective mode field area of the PCF is as large as $1.22084 \times 10^7 \mu\text{m}^2$ at a wavelength of 1,000 μm and a flat dispersion of 0.07669 ± 0.33258 ps/nm/km is obtained. A much lower confinement loss of 6.0253×10^{-16} dB/m is achieved. The single mode transmission over the entire terahertz wave band is described.

Keywords: photonic crystal fiber, low confinement loss, large mode area, terahertz

1. Introduction

The terahertz (THz) frequency ranges from 0.1 THz to 10 THz between microwave and infrared light, corresponding to the wavelength range of 30 μm to 3 mm^[1]. Terahertz waves are promising in THz time domain spectroscopy^[2], THz imaging^[3], security check^[4], astronomy^[5], and biomedical science^[6]. However, one of the challenges confronting terahertz wave transmission is strong transmission loss^[7] and so it is crucial to design a high-efficiency and low-loss THz waveguide. Up to date, many THz waveguides have been proposed and THz metal waveguide have a low absorption loss during propagation of the THz wave propagates^[8,9].

Recently, the photonic crystal fiber (PCF) has attracted much attention as a promising terahertz waveguide boasting high design flexibility. It is a special type with periodically arranged air holes spanning the length of the fiber^[10-12]. PCF possesses excellent features that can not be realized by conventional fibers, for example, high birefringence^[13], endless single-mode transmission^[14], adjustable dispersion^[15], and large effective mode area^[16]. Nielsen et al. designed a terahertz PCF with Topas^[17] and porous-core band gap terahertz PCF^[18] and the losses observed from the two fibers were approximately 0.1 dB/cm and 0.25 dB/cm. R. Pobre et al. studied the single mode characteristics of the Teflon-based PCF and found that the factor affecting the single-mode transmission range was the size of the cladding air holes^[19]. S. Lou et al. designed a hexagonal lattice structure for the polyethylene PCF in THz frequencies and dispersion was close to zero when the frequency was higher than 1 THz^[20]. Owing to the superior characteristics of PCF in terahertz guiding, much effort has been devoted to terahertz PCF waveguides. The large mode area, low confinement loss, and flat dispersion are the objectives being pursued. Recently, it has been shown that PCF with polymeric materials can lower the transmission loss of THz wave. In fact, polymeric materials tend to be cheap and are widely available compared to other dielectrics. For instance, high-density polyethylene (HDPE) and polytetrafluoroethylene (Teflon) have very low transmission losses in the THz band^[21-23] and COC has a small absorption coefficient^[24].

Herein, we describe an octagonal density circle THz-PCF structure with low dispersion, low confinement loss, large mode area, and single-mode transmission over the entire range between 30 μm and 3 mm. The THz-PCF has excellent characteristics and large potential in optical waveguides.

2. Numerical modeling

In this work, a full vectorial finite element method (FEM) was used as the calculation and analytical tool based on the COMSOL Multiphysics software. It has been demonstrated that FEM is applicable to the calculation and analysis of various complex model structures^[25]. Figure 1 shows the schematic diagram of the structure. The blue area represents the base materials of the cyclic olefin copolymer with very low light absorption loss and a refractive index of 1.5258 in the THz band^[26]. The pink area is a perfectly matched layer (PML) for absorption of radiation^[27]. Dense air holes are periodically arranged on the base materials to reduce the refractive index of the cladding. The outer four layers are octagonal and the innermost layer is circular. For the arrangement of air holes, octagonal PCF has many advantages compared with hexagonal PCF. For example, in the single-mode region, the wavelength range is wider, and the distribution of the mode field is closer to the circle and the limiting loss is smaller^[28]. In addition, the innermost air holes are arranged in a circular manner, which is to concentrate more energy on the fiber core and reduce transmission loss. The outer air holes and innermost air hole diameter are, respectively, denoted by d_1 , d_2 and the spacing between layers is denoted as Λ . The distribution of dense circles of the cladding is to better confine light to the core propagation. In order to monitor changes in the distribution of the mode field, the structural parameters are set to be $\Lambda = 400 \mu\text{m}$, $d_1 = 100 \mu\text{m}$, $d_2 = 60 \mu\text{m}$. The fundamental mode distributions in each frequency band are shown in Figure 2 which shows that light is well confined to propagate in the core and the pores have better light confinement capability as the frequency is increased.

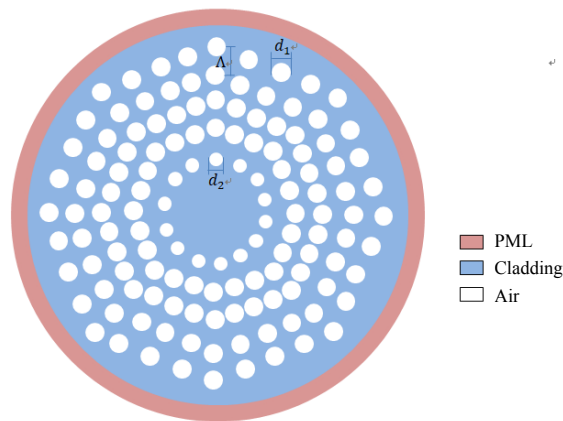


Figure 1. Cross section of the THz-PCF structure

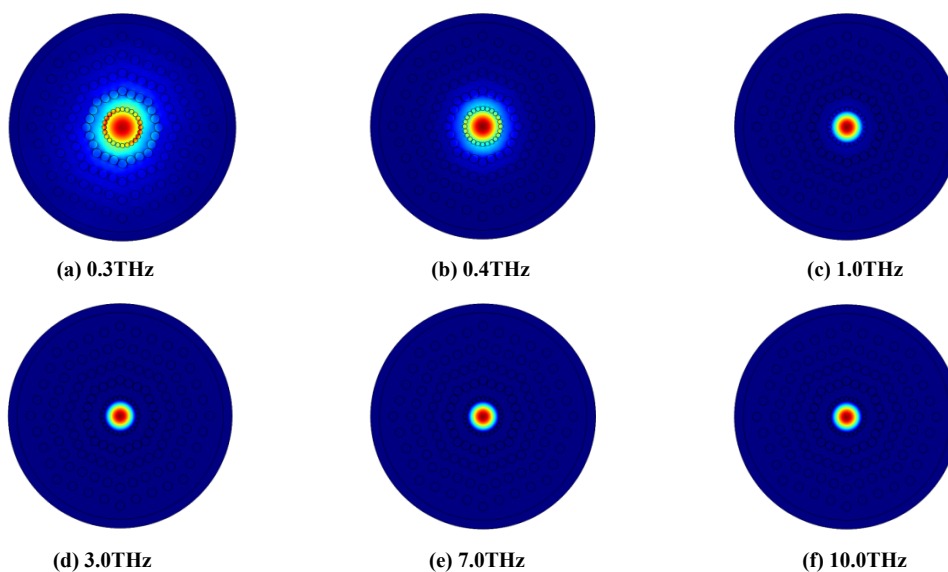


Figure 2. Electric field distribution at different frequencies

The structural parameters of the PCF terahertz waveguide have large influence on the propagation characteristics,

including the single-mode transmission range, effective mode area, dispersion, and transmission loss. These parameters can be optimized by adjusting the structural parameters of the PCF. In general, endless single-mode transmission is crucial to optical fibers because it prevents signal distortion and power loss caused by the transitions between modes. An important indicator of whether a fiber can perform single-mode transmission is the normalized frequency V . For the PCF, the normalized frequency V_{PCF} can be expressed as [29]:

$$V_{PCF} = \frac{2\pi\rho}{\lambda} (n_{co}^2 - n_{eff}^2)^{1/2} \quad (1)$$

where ρ is the equivalent core radius, λ is the vacuum wavelength, n_{co} is the refractive index of the core, and n_{eff} represents the refractive index of the cladding. Because the fiber cross-section is covered with regularly arranged air holes, the fiber cross-section has an equivalent refractive index distribution. This equivalent refractive index is also the equivalent refractive index of the cladding. Since there is no air hole in the core of the PCF, the refractive index of the core is equal to the refractive index of the base material. The normalized frequency is an important factor to realize single-mode transmission in the PCF. In general, the PCF can achieve single-mode transmission when V_{PCF} is less than 2.405^[30].

The effective mode field area is another critical parameter and it is often used to change the nonlinearity of PCF. A large mode field area is expected because it not only performs light transmission, but also reduces the nonlinearity of the PCF. The effective mode field area can be obtained by the following formula^[31]:

$$A_{eff} = \frac{(\iint |E|^2 dx dy)^2}{\iint |E|^4 dx dy} (\mu m^2) \quad (2)$$

where E is the amplitude of the electric field of the basic model. The dispersion of the PCF consists of materials dispersion and waveguide dispersion. In this work, only waveguide dispersion is considered because materials dispersion in the cycloolefin copolymer is close to zero and almost negligible. Dispersion is one of the primary limiting factors of the transmission distance of optical fiber communication systems and hence, flat low dispersion is desirable. Waveguide dispersion of the PCF can be expressed as^[32]:

$$D = -\frac{\lambda}{c} \frac{\partial^2 |\text{Re}(n_{eff})|}{\partial \lambda^2} \quad (3)$$

where c is the light speed in vacuum and $\text{Re}(n_{eff})$ is real part of effective refractive index.

The confinement loss is an important parameter for the fiber THz waveguides. The confinement loss can be calculated from the imaginary part of the effective mode index of refraction obtained from the added PML boundary conditions as expressed in the following^[33]:

$$L_{con} = 8.686k_0 \text{Im}(n_{eff}) \quad (4)$$

where k_0 is the value of $2\pi/\lambda$, $\text{Im}(n_{eff})$ is the imaginary part of the effective mode index.

3. Results and discussion

Figure 3 shows the numerical results of V_{PCF} in the proposed PCFs at different frequencies. It is observed from Figure 3 (a) and Figure 3(b) that the values of V_{PCF} of the PCFs are less than 2.405 regardless of changing d_1 , d_2 , and Λ . This result indicates that the PCF in this study can perform infinite single mode transmission in the THz band. The single-mode transmission range of this model is larger than those results in Ref.^[34].

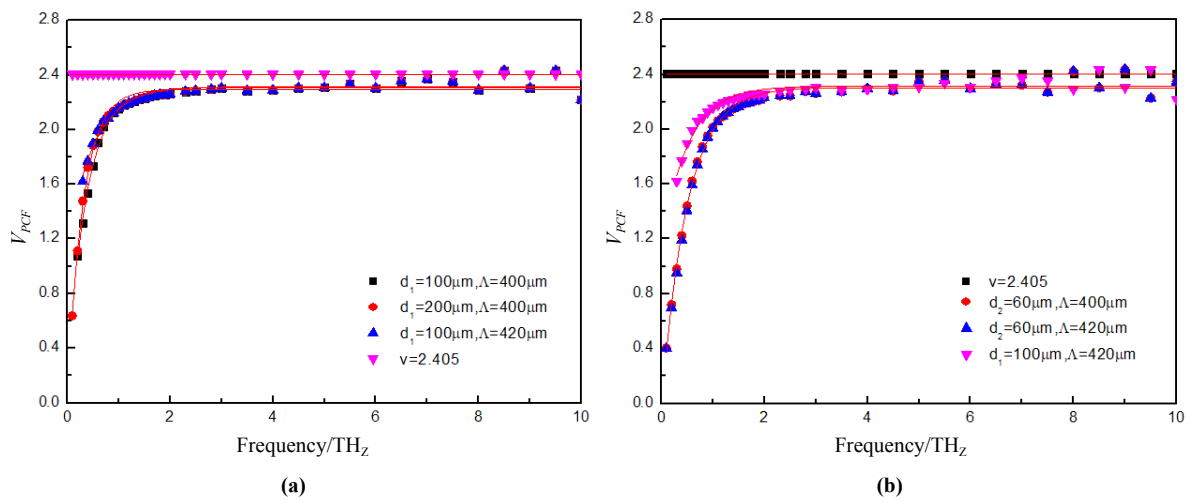


Figure 3. Dependency of V_{PCF} on frequencies for different structural parameters

Figure 4 illustrates the dependence of the effective refractive index of the PCF on frequencies. The real part of the effective refractive index increase initially with frequencies and then reaches a stable value corresponding to the refractive index of the base materials. The imaginary part of the effective mode refractive index decreases with frequency and stabilizes. This phenomenon is attributed to diffusion of the mode field to the cladding at the low frequency band. The restriction power of the cladding increases and energy is confined to the core as the frequency increases.

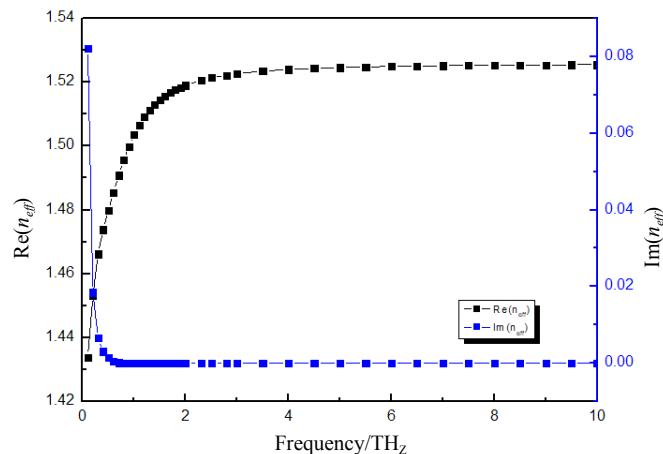


Figure 4. Dependences of the effective refractive index of the PCF on frequencies

Figure 5 shows the variations of the effective mode field areas for different structural parameters of the PCF. Figure 5(a) and 5(b) show that the structural parameters have little effects on the effective mode field area when the wavelength is less than $375 \mu\text{m}$. However, influences of the structural parameters on the effective mode field area are more obvious when the wavelength is larger than $375 \mu\text{m}$. It can be seen from the results shown in Figure 5 that the binding light beams ability of the THz wave is weakened when the wavelengths exceed $400 \mu\text{m}$, which causes more energy to diffuse into the cladding, thus leading to be a sharp increase in the effective mode field area. The maximum effective mode field area at a wavelength of $1,000 \mu\text{m}$ is $1.41868 \times 10^7 \mu\text{m}^2$ for $d_1 = 100 \mu\text{m}$, $d_2 = 100 \mu\text{m}$, and $\Lambda = 400 \mu\text{m}$, as shown in Figure 5(a). In addition, Figure 5(b) shows that d_2 has a greater influence on the effective mode field area. When d_1 , d_2 , and Λ are $100 \mu\text{m}$, $100 \mu\text{m}$ and $420 \mu\text{m}$, respectively, the effective mode field area reaches $1.22084 \times 10^7 \mu\text{m}^2$ at $1,000 \mu\text{m}$, and the values are much larger than those in Refs. [35] and [36].

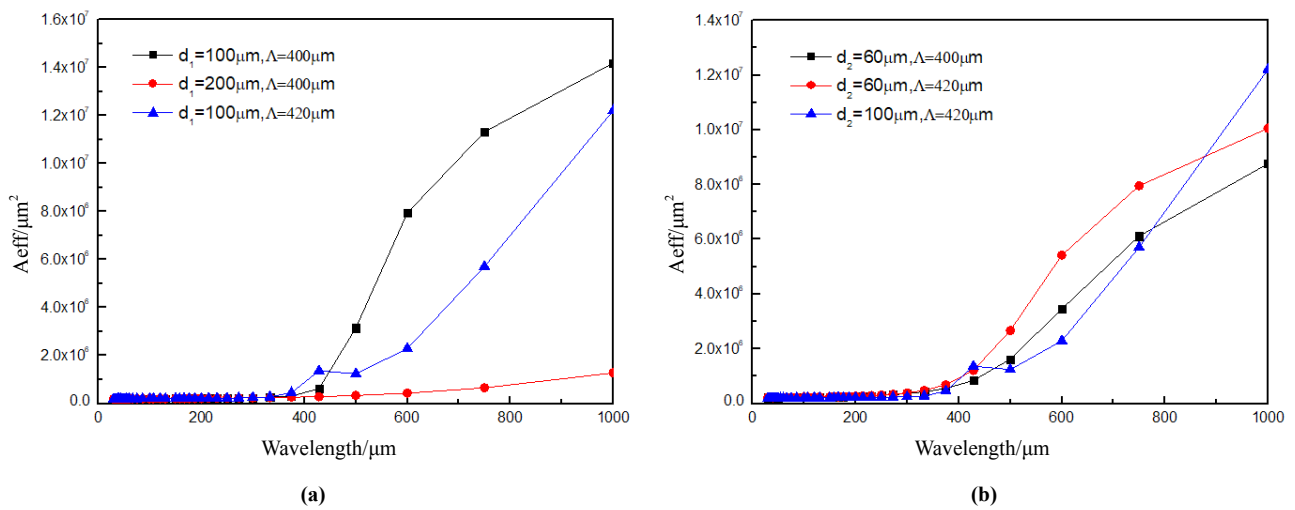


Figure 5. Variations of effective mode field areas for various parameters of the PCF

Figure 6 shows the dispersion characteristics of the PCF with different structural parameters in the terahertz region. As shown in Figure 6(a), the black curve is relatively flat indicating that dispersion is small in this wavelength range. Figure 6(b) shows that d_2 has a larger effect on dispersion. The ultra-flat dispersion of 0.07669 ± 0.33258 ps/nm/km is obtained in the entire THz band for $d_1 = 100 \mu m$, $d_2 = 60 \mu m$, and $\Lambda = 400 \mu m$. The dispersion obtained from this structure is flatter and smaller than the results in Refs. [37] and [38].

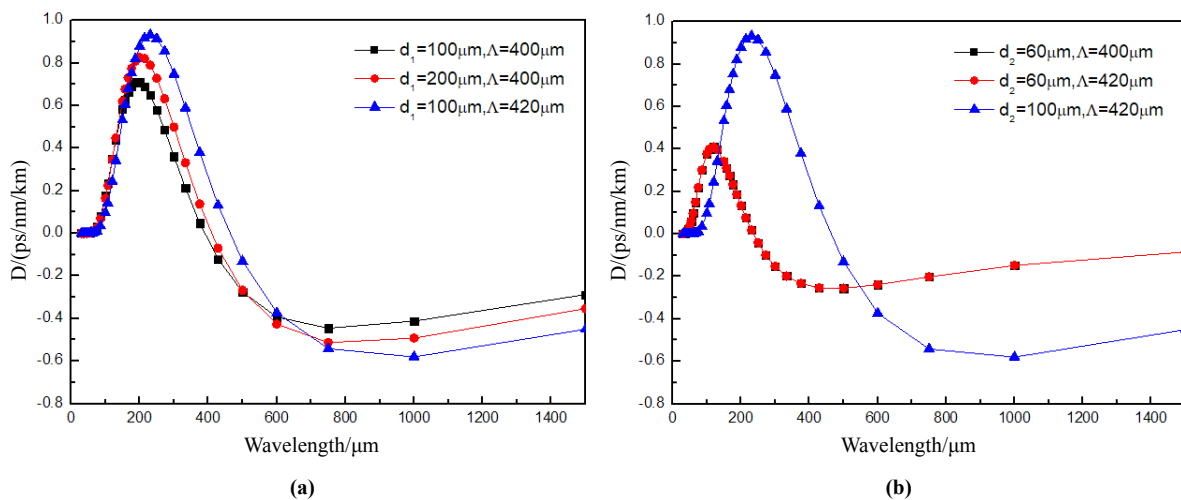


Figure 6. Dispersion characteristics of the PCF for different structure parameters in terahertz region

The confinement loss characteristics of the THz-PCF are shown in Figure 7. The structural parameters are $d_1 = 200 \mu m$, $d_2 = 100 \mu m$, and $\Lambda = 400 \mu m$. The confinement loss increases with increasing wavelengths when the wavelength is larger than a specific value. The confinement loss is low between $30 \mu m$ and $334 \mu m$ and a minimum confinement loss of 6.0253×10^{-16} dB/m can be achieved at $214 \mu m$. The obtained confinement loss is smaller than those described in Refs. [34] and [39]. Obviously, it can be known from Figure 7 that d_1 and d_2 have higher effect on confinement loss than air holes spacing.

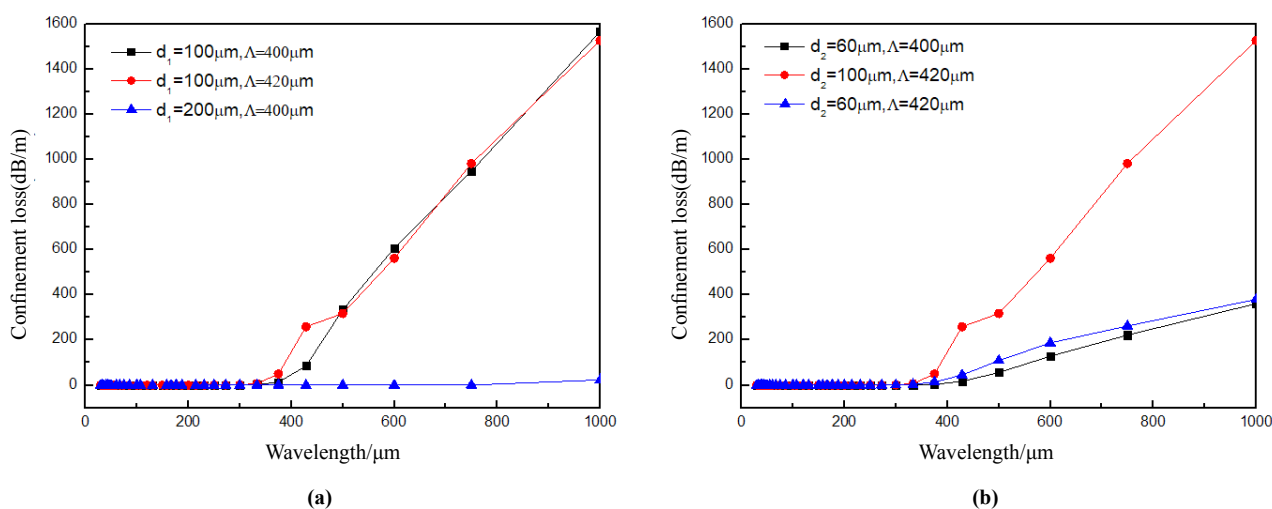


Figure 7. Confinement losses characteristics of the THz-PCF under different structural parameters

4. Conclusion

A THz-PCF made of COC boasting low dispersion and confinement loss, large-mode-area, and single mode transmission over the entire THz range is described. Our results show that the effective mode field area is as large as $1.22084 \times 10^7 \mu\text{m}^2$ at $1,000 \mu\text{m}$ together with an ultra-flat dispersion of $0.07669 \pm 0.33258 \text{ ps/nm/km}$. A confinement loss of $6.0253 \times 10^{-16} \text{ dB/m}$ is achieved at $214 \mu\text{m}$. Single-mode transmission is realized over the entire THz wave band and this THz-PCF has superior characteristics. The PCF terahertz wave guiding proposed in this work can be used in wireless communication and long-distance optical signal transmission.

5. Acknowledgments

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